

## MATH 1314

### Chapter 3.4: Zeros Of Polynomial Functions

Find all zeros of  $f(x) = x^3 + 2x^2 - 5x - 6$ .

Rational Zeros Theorem:

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$$

Factors of P =  $a_0$

-----  $\rightarrow$  Possible zeros of  $f(x)$

Factors of Q =  $a_n$

Find all zeros of  $f(x) = x^3 + 2x^2 - 5x - 6$ .

Find all zeros of  $f(x) = x^3 + 7x^2 + 11x - 3$ .

Find all zeros of  $f(x) = x^4 - 6x^2 - 8x + 24$ .

### Fundamental Theorem Of Algebra:

A polynomial of degree  $N$  has a maximum of  $N$  real roots.

$f(x) = 0$  has at least one complex root  $a + bi$ .

### Descartes' Rule Of Signs

Positive Real Zeros:

the number of sign changes  $N$  of  $f(x)$  or  $N - \text{Even Number}$

Negative Real Zeros:

the number of sign changes  $N$  of  $f(-x)$  or  $N - \text{Even Number}$

Find the number of possible positive and negative zeros of

$$f(x) = 3x^7 - 2x^5 - x^4 + 7x^2 + x - 3.$$

Find the number of possible positive and negative zeros of

$$f(x) = x^3 + 2x^2 + 5x + 4.$$